57.162 mm. having been determinated by calibration with sodium chloride. The dimensions of the unit cell were found to be:

$$a_0 = 7 \cdot 37 \pm 0.02, \ b_0 = 4 \cdot 60 \pm 0.02, \ c_0 = 14 \cdot 34 \pm 0.03 \text{ Å};$$
  
$$\beta = 108^\circ 59' \pm 8'.$$

These data give the axial ratios: a:b:c=1.602:1:3.118. The observed density of 1.42 g.cm.<sup>-3</sup> agrees well with the density of 1.417 g.cm.<sup>-3</sup> calculated on the basis of two formula units per unit cell.

When the diffraction spots in the Weissenberg and

precession photographs were indexed the following interferences were observed: hkl in all orders; h0l when l=2n; 0k0 when k=2n. These data are consistent with the space group  $C_{2h}^{5}-P2_{1}/c$ . Structural investigations on 5-oxiphenazine and 5-10-dioxiphenazine are in progress.

## Reference

WOHL, A. & AUE, W. (1901). Ber. dtsch. chem. Ges. 34, 2446.

Acta Cryst. (1960). 13, 56

# The crystal structure of Zr<sub>4</sub>Al<sub>3</sub>. By C. G. Wilson, D. K. THOMAS and F. J. SPOONER, Royal Military College of Science, Shrivenham, Berks, England

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The crystal structure of the intermetallic compound  $Zr_4Al_3$  has been determined from powder photographs. Powder specimens were obtained by filing from a solid sample of the alloy prepared by arc melting in argon by Miss J. Murray, A.E.R.E., Harwell. Microscopic examination of a polished surface of the solid sample shewed it to be mainly single phase. The photographs

#### Table 1. X-ray data

(hkl)	$\sin^2 \theta$ (obs.)	$\sin^2 \theta$ (calc.)	Intensities (obs.)	Intensities (calc.)
0001	0.0204	0.0204	m	2.3
1010	0.0268	0.0268	m	2.7
1011	0.0472	0.0473	m	2.9
$11\overline{2}0$	0.0805	0.0805	vs	18.4
0002	0.0817	0.0818	งขบ	0.4
1121	0.1009	0.1010	vs	10.3
$20\overline{2}0$	0.1073	0.1074	ms	3.1
1012	0.1086	0.1086	vs	19.0
$20\overline{2}1$	0.1277	0.1278	ms	4.9
$20\overline{2}2$	0.1887	0.1888	m	3.3
2131	0.2079	0.2080	vw	0.6
1013	0.2104	0.2105	vvw	0.3
3030	0.2412	0.2412	m	3.4
$30\overline{3}1$	0.2615	0.2616	m	$2 \cdot 3$
$11\overline{2}3$	0.2640	0.2614	m	2.2
2132	0.2692	0.2692	8	8.9
$20\bar{2}3$	0.2909	0.2909	w	1.3
$22\overline{4}0$	0.3216	0.3216	m	3.6
0004	0.3267	0.3266	vw	1.2
$22\overline{4}1$	0.3422	0.3420	vvw	0.3
3141	0.3684	0.3688	างงาง	0.2
2133	0.3711	0.3713	1717117	0.2
$22\overline{4}2$	0.4034	0.4032	จากกาย	0.16
$11\overline{2}4$	0.4071	0.4070	m	2.9
3033	0.4250	0.4249	าามา	1.0
$31\bar{4}2$	0.4302	0.4299	ms	4.1
2024	0.4339	0.4336	1110	0.6
4041	0.4490	0.4492	1717117	0.7
4042)	0 2102	0.5104		
0005	0.2102	0.5105	w	0.8
3143 ′	0.5323	0.5321	vvvw	0.16

vs=very strong; s=strong; ms=medium strong; m=medium; w=weak; vw=very weak:

vvw=very very weak; vvvw=extremely weak.

obtained with a precision 19 cm. camera (Adam, 1954) gave fairly broad lines with a heavy background caused by the Zr  $K\alpha$  radiation excited by the continuous spectrum of the Cu target. Whilst these photographs enabled a unit cell to be determined, more accurate measurements of line spacings and intensities were made on a photograph taken by Dr J. Adam with a focusing camera using monochromatised Cu  $K\alpha$  radiation. An attempt was made to find single crystals of suitable size in a crushed specimen, but this proved impossible. The values of  $\sin^2 \theta$ obtained from measurements made with a Cambridge universal measuring machine and the visual estimate of line intensities is given in Table 1.

Several weak and very weak lines appearing on the focusing camera film have been shown to belong to a neighbouring phase in the Zr-Al system. All the remaining lines have been indexed on a hexagonal unit cell with:

 $a = 5.433 \pm 0.002, \ c = 5.390 \pm 0.002 \text{ Å}$ .

Assuming that the volumes occupied by the individual atoms in the alloy are not appreciably different from those occupied by these atoms in the elements, the number of formula units of  $Zr_4Al_3$  per unit cell is unity. On this basis the calculated density is 5.37 g.cm.<sup>-3</sup>. The density of the solid sample determined using a specific-gravity bottle was 5.28 g.cm.<sup>-3</sup>.

No systematic absences were observed and packing considerations led to a choice of space group  $C_{3h}^{1}-P\overline{6}$ . The calculated line intensities shown in Table 1 are obtained with the atoms in the following positions:

3 Al 2(j) x, y, 0; with  $x = \frac{1}{3}, y = \frac{1}{6}$ . 2 Zr 3(h)  $\frac{1}{3}, \frac{2}{3}, z$ ; with  $z = \frac{1}{4}$ . 1 Zr  $\overline{6}(f)$   $\frac{2}{3}, \frac{1}{3}, \frac{1}{2}$ . 1 Zr  $\overline{6}(b)$  0, 0,  $\frac{1}{2}$ .

The interatomic distances are as follows:

(6) Al–Zr	3∙03 Å
(6) Zr–Zr	3.41
(l) Zr–Zr	2.70
(2) Al–Al	2.72





Fig. 1. Structure of (a)  $Zr_4Al_3$  and (b)  $\sigma$ -phase (Fe-Cr).

The proposed structure bears a close resemblance to the  $\sigma$ -phase structure of the transition elements. A section of the structure viewed along the c-axis is shown in Fig. 1, together with a similar section of the  $\sigma$ -phase of Fe-Cr. In the  $\sigma$ -phase the two layers of atoms having pseudo-hexagonal symmetry have their hexagonal axes displaced relative to each other, whilst the corresponding layers of alternate Zr and Al atoms in the Zr<sub>4</sub>Al<sub>3</sub> structure are symmetrically disposed relative to each other about the common hexagonal axis.

The Zr atoms in the  $\frac{1}{3}, \frac{2}{3}, \pm \frac{1}{4}$ , positions form an unbroken chain as in the  $\sigma$ -phase. The distance between the Zr atoms in this chain is 2.7 Å, which is much less than the normal 12-co-ordination interatomic distance (3.2 Å approx.) for Zr. This atomic compression, which is also apparent in the  $\sigma$ -phase, may possibly be explained by the comparative isolation of the similar chains of atoms.

### Discussion

It is interesting to note that the  $Zr_4Al_3$  structure is identical with the structure for  $A_4B_3$  alloys postulated by Frank & Kasper in a recent paper (Frank & Kasper, 1959). In their paper Frank & Kasper discuss the analysis and classification of complex alloys on the basis of sphere packing using the concept of triangulated coordination shells. The main properties of these co-ordination shells were discussed in an earlier paper (Frank & Kasper, 1958).

The new  $A_4B_3$  structure is regarded by Frank & Kasper as a modification of the CaZn<sub>5</sub> structure in which the Ca atoms, which lie along the hexagonal axes of the simple kagomé net at z = 0, are replaced by two smaller atoms at  $z = \frac{1}{4}$  and  $z = \frac{3}{4}$ . In the case of  $Zr_4Al_3$  the Ca atoms are replaced by Zr atoms  $(\frac{1}{3}, \frac{2}{3}, \frac{1}{4} \text{ and } \frac{1}{3}, \frac{2}{3}, \frac{3}{4})$ . The Zn' and Zn'' atoms of the CaZn<sub>5</sub> structure are replaced by Al atoms at  $(\frac{1}{3}, \frac{1}{6}, 0)$  and Zr atoms at  $(\frac{2}{3}, \frac{1}{3}, \frac{1}{2})$ , respectively, in the  $Zr_4Al_3$  structure. The Zr atoms in the  $z = \frac{1}{4}$  and  $z = \frac{3}{4}$  positions have an asymmetrical Z14 co-ordination shell which is oblate and leads to the apparent compression of the Zr atoms. According to Frank & Kasper such Z14 co-ordination shells are generally oblate and normally occupied by the atoms of transition elements. As far as is known Zr<sub>4</sub>Al<sub>3</sub> is the first compound to be reported having the new structure and this would appear to add some force to the new concepts governing the structure of complex alloys enunciated by Frank & Kasper.

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#### References

ADAM, J. (1954). J. Sci. Instrum. 31, 131. FRANK, F. C. & KASPER, J. S. (1958). Acta Cryst. 11, 184. FRANK, F. C. & KASPER, J. S. (1959). Acta Cryst. 12, 483.